



Informed Meta-Learning Learning the inductive bias from human expert knowledge

Katarzyna Kobalczyk

Mihaela van der Schaar

Department of Applied Mathematics and Theoretical Physics, University of Cambridge, Cambridge CB3 0WA, United Kingdom

Introduction

Informed machine-learning: from knowledge to inductive biases. Machine learning practitioners map expert knowledge to prior probabilities over functions by manual model design. Regions of the function space with a non-zero prior probability define the hypothesis space and the relative probabilities of prior solutions dictate the inductive biases of the model. Knowledge about different learning tasks is associated with distinct inductive biases. Models with well-designed task-specific **Pros:** biases require less training data and are more robust. Cons: Handcrafted biases require significant engineering efforts and need to be customized for every new learning problem.



Data efficiency, robustness and uncertainty. f(x) = ax + sin(bx) + c f(x) = ax + sin(bx) + c

Meta-learning as inductive bias learning. Instead of manual inductive bias specification, the paradigm of meta-learning proposes that inductive biases are meta-learned by training over a distribution of related tasks.

Pros: Meta-learning enables flexible learning of complex inductive biases otherwise difficult to design by hand.

Cons: Success of meta-learners depends on the similarity of tasks at meta-train and test time. Heterogenous task distributions fail to provide strong inductive biases.

 h_1



 x_i

 y_i



In informed meta-learning the mapping from knowledge to inductive biases, $\mathcal{K} \to p(f | \mathcal{K})$, is meta-learned by training over multiple learning tasks and their representations of knowledge.

 f_1^* f_2^* Hypothesis space Heterogeneous environments span a wide range of functions, and thus support a wider range of tasks,



concentrating the meta-distribution around the task-relevant regions.



On a series of controlled synthetic experiments, we:

- Demonstrate how successful integration of oracle knowledge about the data generating process improves data efficiency and mitigate the adverse effects of train-test distribution shift.
- We derive methods to quantitatively measure the **impact of expert knowledge on the reduction in epistemic uncertainty.**

From natural language to functional priors. In practical scenarios, predictive functions are difficult to model with closed-form mathematical expressions. The benefit of meta-learned prior is their functional flexibility. We show how INPs learn to map descriptions in natural language to functional priors.



The night will start off cold with temperatures falling to -8.9°C by late morning, and then gradually rise to a high of 1.6°C in the late afternoon. Temperatures will start to drop again in the evening, reaching -3.1°C by midnight.

The night will start off chilly with temperatures around 0.5° C, but it will drop to -1.7° C by early morning. The day will gradually warm up, reaching a high of 5.1° C in the afternoon before cooling off to 1.0° C by midnight.

The night will start off cold with temperatures falling to -16.8°C by dawn, and the day will continue to get colder, reaching a chilly -23.0°C by midnight. Afternoon temperatures will hover around -18.5°C, so bundle up if you're heading out.

The night will be bitterly cold with temperatures around -18 degrees, gradually increasing to -14 degrees by late afternoon. The temperature will slightly drop again to -15 degrees in the evening, warming up a bit to -14 degrees at midnight.





Method

Informed Neural Processes. We instantiate an informed meta-learner by extending the family of Neural Processes—probabilistic, fully amortized meta-learners.

Model. (I)NPs model the distribution over functions through a fixed dimensional latent variable z sampled from a variational distribution q. INPs extend NPs by additionally conditioning q on the information contained in expert knowledge. We model the predictive posterior distribution as:

$$p(y \mid x, \mathcal{D}_C, \mathcal{K}) := \int p(y \mid x, z) q(z \mid \mathcal{D}_C, \mathcal{K}) dz$$

Training. INPs are trained in an episodic fashion over a distribution of learning task $\mathcal{T}_j = \{\mathcal{D}_C, \mathcal{D}_T\}$ and their associated knowledge representations \mathcal{K}_j . Denoting by r_C and r_T the context and target data representations and by k the knowledge embedding vector of a single task, parameters of the model are learned by maximising the expectation of ELBO over all training tasks,

 $\log p(y_T \mid x_T, r_C, k) \ge \mathbb{E}_{q(z \mid r_T, k)} \left[\log p(y_T \mid x_T, z) \right] - D_{\text{KL}} \left(q(z \mid r_T, k) \mid \mid q(z \mid r_C, k) \right)$

Beyond 1D regression. We extend INPs to the task of few-shot classification with expert knowledge in the form class-level features or descriptions in natural language. Successful alignment of knowledge and data representations facilitates robust generalization to new, previously unseen classes, zero-shot classification and improved few-shot classification accuracy.

